

# Package: crann (via r-universe)

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**Title** Spanning Tree Methods for Graphs

**Version** 0.0.1

**Description** Implements spanning tree algorithms for undirected graphs represented as 'adj' adjacency lists. Provides enumeration of all spanning trees via Winter's (1986) contraction-based algorithm <doi:10.1007/BF01939361>, counting via Kirchhoff's matrix tree theorem, minimum spanning trees via Kruskal's algorithm, uniform random sampling via Wilson's (1996) loop-erased random walk <doi:10.1145/237814.237880>, and structural utilities including fundamental cycles and cuts.

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count\_spanning\_trees *Count spanning trees*

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## Description

Counts the number of spanning trees of a connected undirected graph using Kirchhoff's matrix tree theorem: the count equals the determinant of any  $(n-1) \times (n-1)$  cofactor of the graph Laplacian.

## Usage

```
count_spanning_trees(graph)
```

## Arguments

graph            An adj object representing a connected undirected graph.

## Value

A numeric scalar. (Integer-valued but returned as numeric since counts can exceed `.Machine$integer.max` for dense graphs.)

## See Also

[enumerate\\_spanning\\_trees\(\)](#) to list all spanning trees.

## Examples

```
# Triangle: 3 spanning trees
g <- adj::adj(list(c(2L, 3L), c(1L, 3L), c(1L, 2L)))
count_spanning_trees(g)
```

---

`enumerate_spanning_trees`*Enumerate all spanning trees*

---

**Description**

Enumerates all spanning trees of a connected undirected graph using Winter's (1986) contraction-based algorithm. The algorithm has worst-case time complexity  $O(n + m + nt)$  and space complexity  $O(n^2)$ , where  $n$  is the number of vertices,  $m$  the number of edges, and  $t$  the number of spanning trees.

**Usage**

```
enumerate_spanning_trees(graph)
```

**Arguments**

<code>graph</code>	An adj object representing a connected undirected graph without self-loops or duplicate edges.
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**Value**

A list of adj objects, one per spanning tree.

**References**

Winter, P. (1986). An algorithm for the enumeration of spanning trees. *BIT Numerical Mathematics*, 26(1), 44–62. doi:[10.1007/BF01939361](https://doi.org/10.1007/BF01939361)

**Examples**

```
# Triangle: 3 spanning trees
g <- adj::adj(list(c(2L, 3L), c(1L, 3L), c(1L, 2L)))
trees <- enumerate_spanning_trees(g)
length(trees)
```

---

`enumerate_spanning_trees_edges`*Enumerate spanning trees as an edge matrix*

---

**Description**

Returns a compact integer matrix encoding all spanning trees of a connected undirected graph. The matrix has  $n-1$  rows and  $2t$  columns, where  $n$  is the number of vertices and  $t$  is the number of spanning trees. For spanning tree  $k$  (1-indexed), columns  $2k-1$  and  $2k$  hold the  $u$  and  $v$  endpoints (1-indexed vertex IDs) of each of the  $n-1$  edges.

**Usage**

```
enumerate_spanning_trees_edges(graph)
```

**Arguments**

graph            An adj object representing a connected undirected graph without self-loops or duplicate edges.

**Details**

This function is substantially faster than `enumerate_spanning_trees()` for graphs with many spanning trees because it avoids per-tree R memory allocation: the entire output is a single integer matrix allocation.

**Value**

An integer matrix with  $n-1$  rows and  $2t$  columns.

**References**

Winter, P. (1986). An algorithm for the enumeration of spanning trees. *BIT Numerical Mathematics*, 26(1), 44–62. doi:[10.1007/BF01939361](https://doi.org/10.1007/BF01939361)

**Examples**

```
# Triangle: 3 spanning trees, 2 edges each -> 2 x 6 matrix
g <- adj::adj(list(c(2L, 3L), c(1L, 3L), c(1L, 2L)))
enumerate_spanning_trees_edges(g)
```

---

fundamental_cuts	<i>Fundamental cuts of a spanning tree</i>
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---

**Description**

Returns the fundamental cuts of a spanning tree with respect to the original graph. There is one fundamental cut per tree edge ( $n - 1$  total), consisting of all edges in the graph that cross the bipartition induced by removing that tree edge.

**Usage**

```
fundamental_cuts(graph, tree)
```

**Arguments**

graph            An adj object representing a connected undirected graph.  
tree             An adj object representing a spanning tree of graph.

**Value**

A list of adj objects, one per tree edge. Each adj represents the cut as a subgraph of graph.

**See Also**

[fundamental\\_cycles\(\)](#)

**Examples**

```
g <- adj::adj(list(c(2L, 3L), c(1L, 3L), c(1L, 2L)))
t <- minimum_spanning_tree(g)
fundamental_cuts(g, t)
```

---

`fundamental_cycles`      *Fundamental cycles of a spanning tree*

---

**Description**

Returns the fundamental cycles of a spanning tree with respect to the original graph. There is one fundamental cycle per non-tree edge ( $m - n + 1$  total), formed by adding that edge to the unique path between its endpoints in the spanning tree.

**Usage**

```
fundamental_cycles(graph, tree)
```

**Arguments**

`graph`            An adj object representing a connected undirected graph.  
`tree`             An adj object representing a spanning tree of graph.

**Value**

A list of adj objects, one per non-tree edge. Each adj represents the cycle as a subgraph of graph.

**See Also**

[fundamental\\_cuts\(\)](#)

**Examples**

```
g <- adj::adj(list(c(2L, 3L), c(1L, 3L), c(1L, 2L)))
t <- minimum_spanning_tree(g)
fundamental_cycles(g, t)
```

---

is\_spanning\_tree      *Test if a graph is a spanning tree*

---

### Description

Returns TRUE if tree is a spanning tree: a connected acyclic graph with exactly n-1 edges. To additionally check that tree uses only edges from a reference graph, see [is\\_spanning\\_tree\\_of\(\)](#).

### Usage

```
is_spanning_tree(tree)
```

### Arguments

tree                    An adj object to test.

### Value

A logical scalar.

### See Also

[is\\_spanning\\_tree\\_of\(\)](#), [minimum\\_spanning\\_tree\(\)](#), [enumerate\\_spanning\\_trees\(\)](#)

### Examples

```
g <- adj::adj(list(c(2L, 3L), c(1L, 3L), c(1L, 2L)))
t <- minimum_spanning_tree(g)
is_spanning_tree(t)
```

---

is\_spanning\_tree\_of      *Test if a graph is a spanning tree of another graph*

---

### Description

Returns TRUE if tree is a spanning tree of graph: a connected acyclic subgraph that spans all vertices and uses only edges present in graph.

### Usage

```
is_spanning_tree_of(tree, graph)
```

### Arguments

tree                    An adj object to test.  
graph                   An adj object representing a connected undirected graph.

**Value**

A logical scalar.

**See Also**

[is\\_spanning\\_tree\(\)](#), [minimum\\_spanning\\_tree\(\)](#), [enumerate\\_spanning\\_trees\(\)](#)

**Examples**

```
g <- adj::adj(list(c(2L, 3L), c(1L, 3L), c(1L, 2L)))
t <- minimum_spanning_tree(g)
is_spanning_tree_of(t, g)
```

---

minimum\_spanning\_tree *Minimum spanning tree*

---

**Description**

Finds a minimum spanning tree of a connected undirected graph using Kruskal's algorithm. When weights is NULL (the default), all edges are treated as having equal weight and any spanning tree is returned.

**Usage**

```
minimum_spanning_tree(graph, weights = NULL)
```

**Arguments**

graph	An adj object representing a connected undirected graph.
weights	A numeric vector of edge weights, one per edge. Edges are ordered by iterating vertices $u = 1, \dots, n$ and for each $u$ iterating over $\text{graph}[[u]]$ retaining only neighbors $v > u$ . Pass NULL for uniform weights.

**Value**

An adj object representing the minimum spanning tree.

**See Also**

[is\\_spanning\\_tree\(\)](#) to validate a spanning tree.

**Examples**

```
g <- adj::adj(list(c(2L, 3L), c(1L, 3L), c(1L, 2L)))
minimum_spanning_tree(g)
```

---

sample\_spanning\_tree *Sample a uniform random spanning tree*

---

**Description**

Samples a spanning tree uniformly at random from the set of all spanning trees using Wilson's (1996) loop-erased random walk algorithm.

**Usage**

```
sample_spanning_tree(graph)
```

**Arguments**

graph            An adj object representing a connected undirected graph.

**Value**

An adj object representing a spanning tree of graph.

**References**

Wilson, D.B. (1996). Generating random spanning trees more quickly than the cover time. *Proceedings of the 28th Annual ACM Symposium on Theory of Computing*, 296–303. doi:[10.1145/237814.237880](https://doi.org/10.1145/237814.237880)

**See Also**

[enumerate\\_spanning\\_trees\(\)](#), [minimum\\_spanning\\_tree\(\)](#)

**Examples**

```
set.seed(1)
g <- adj::adj(list(c(2L, 3L), c(1L, 3L), c(1L, 2L)))
sample_spanning_tree(g)
```

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